

9. (1) $\overline{OC} = 1 \text{ m}$ ，故彈簧自由長度 = $1 - 0.3 = 0.7 \text{ m}$
 $\overline{OB} = 1 \cos 45^\circ = 0.7071 \text{ m}$ ，此時彈簧伸長量為 0.0071 m
 彈性功 + 重力功 = 位能差

$$\frac{1}{2}(500)(0.3)^2 - \frac{1}{2}(500)(0.0071)^2 + 2(9.81)(0.5) = \frac{1}{2}(2)(v_B^2)$$

$$\Rightarrow v_B = 5.7 \text{ m/s}$$

(2) $2(9.81)(1) = \frac{1}{2}(2)v_A^2$
 $v_A = 4.43 \text{ m/s}$

10. 設前行距離為 $x \text{ m}$

$$\frac{1}{2}(1500)(0.65)^2 + \frac{1}{2}(15)(10)^2 = (0.2)(15)(9.81)(2.5 + x) + \frac{1}{2}(1500)(0.63 + x)^2$$

解上式得 $x = 0.5 \text{ m}$

11. $y_P = 3(-3)^2 = 27 \text{ m}$
 $y_Q = 3(1)^2 = 3 \text{ m}$

$$\therefore m(9.81)(27 - 3) = \frac{1}{2}mv_Q^2$$

$$\Rightarrow v_Q = 21.7 \text{ m/s}$$

$$\left. \frac{dy}{dx} \right|_{x=1} = 6 = \tan \theta, v_{Qx} = 3.57 \text{ m/s}$$

$$\Rightarrow \theta = 80.54^\circ, v_{Qy} = 21.4 \text{ m/s}$$

離開 Q 後繼續往上飛 $t_1 \text{ s}$

$$t_1 = \frac{21.4}{9.81} = 2.181 \text{ s}$$

回落到點 Q 之高度共花了 $2t \text{ s} = 4.363 \text{ s}$

如繼續用了 $t \text{ s}$ 從 Q 落到 $y=0$ 位置，則

$$3 = 21.4t + \frac{1}{2}(9.81)t^2 \Rightarrow t = 0.136 \text{ s}$$

所以， R 之 x 座標 = $3.57(4.363 + 0.136) + 1 = 17.06$

12. (1) 當球來到任一高度 h 的點 B 時，其速度 v_B ：

$$mg(L - h) = \frac{1}{2}mv_B^2 \Rightarrow v_B^2 = 2g(L - h)$$

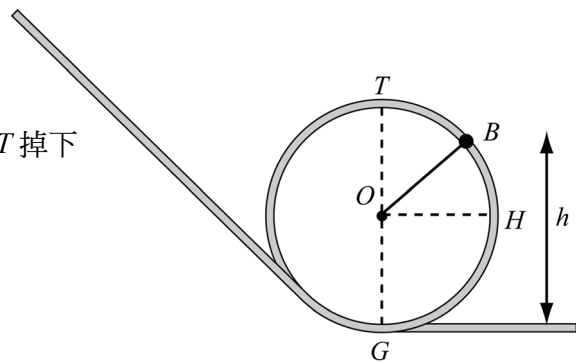
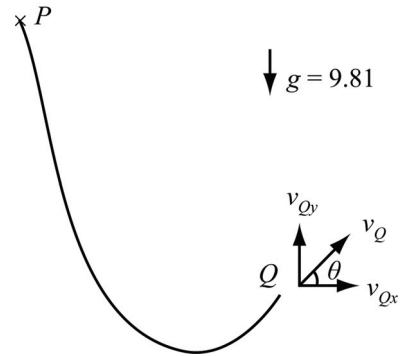
$$\text{其離心力} = m \frac{v_B^2}{r} = \frac{4mg(L - h)}{d}$$

此離心力最小要為 mg ，才不致在最高點 T 掉下

$$\therefore mg = \frac{4mg(L - d)}{d} \Rightarrow L = \frac{5}{4}d \text{ m}$$

(2) 在 H 點， $v_H = 2g\left(L - \frac{d}{2}\right)$

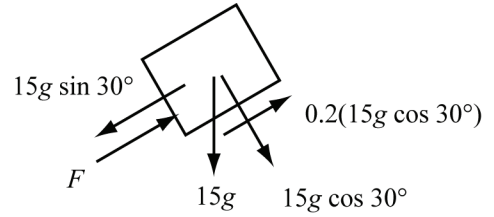
$$\text{軌道反作用力} = \text{離心力} = \frac{4mg\left(L - \frac{d}{2}\right)}{d} = \frac{2mg(2L - d)}{d} \text{ N}$$



13. $F = 15g \sin 30^\circ + (0.2)(15g \cos 30^\circ) = 99.1 \text{ N}$

所以，其功率 = $Fv = 495.3 \text{ W}$

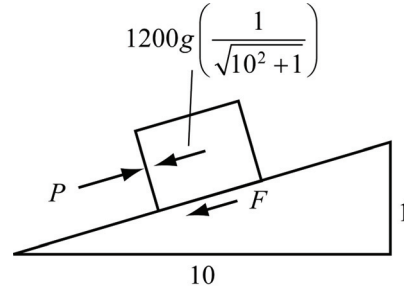
$$\text{機械效率} = \frac{(15g \sin 30^\circ)(5)}{495.3} \times 100\% = 74\%$$



14. 車行之阻力 $F: F \left(\frac{40 \times 10^3}{3600} \right) = 3300 \Rightarrow F = 297 \text{ N}$

$$P = 1200g \left(\frac{1}{\sqrt{10^2 + 1}} \right) + F = 1468.4 \text{ N}$$

$$\therefore Pv = 3300 \Rightarrow v = 2.25 \text{ m/s} = 8.1 \text{ km/hr}$$



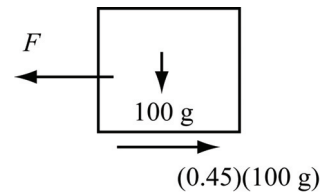
15. 功率 = $(1100 - 950)(9.81)(0.5) = 735.75 \text{ W}$

16. $v^2 = v_0^2 + 2as \Rightarrow 3^2 = 0^2 + 2a(15) \Rightarrow a = 0.3 \text{ m/s}^2$

$$F - 0.45(100g) = 100(0.3) \Rightarrow F = 471.45$$

所以，輸出功率 = $Fv = (471.45)(3) = 1414.4 \text{ W}$

$$\Rightarrow \text{輸入功率} = \frac{1414.4}{0.75} = 1886 \text{ W}$$



17. 當套筒自 $\theta = 90^\circ$ 狀態滑下至某 θ

$$\text{彈簧伸長量} = \frac{1.5}{\cos \theta} - 1.5 = (1.5) \left(\frac{1 - \cos \theta}{\cos \theta} \right)$$

$$v(\theta) = -20g(1.5 \tan \theta) + \frac{1}{2}k(1.5)^2 \left(\frac{1 - \cos \theta}{\cos \theta} \right)^2$$

$$= -294.3 \tan \theta + 1.125k \left(\frac{1 - \cos \theta}{\cos \theta} \right)^2$$

$$v(50^\circ) = 0 = -350.73 + 0.347k \Rightarrow k = 1009.5 \text{ N/m}$$

18. 由伸長量 x_1 到 x_2 彈簧力所作功

$$U_{1 \rightarrow 2} = \int_{x_1}^{x_2} -(ax + bx^2) dx = - \left[\frac{ax^2}{2} + \frac{bx^3}{3} \right]_{x_1}^{x_2} = \left(\frac{ax_1^2}{2} + \frac{bx_1^3}{3} \right) - \left(\frac{ax_2^2}{2} + \frac{bx_2^3}{3} \right)$$

$$\therefore v_e = \frac{ax^2}{2} + \frac{bx^3}{3}$$

19. $U_{0 \rightarrow 1} = mgR^2 \left(\frac{1}{r_1} - \frac{1}{r_0} \right)$

$$= m(9.81)(6370 \times 10^3)^2 \left[\frac{10^{-3}}{(6370 + 1300)} - \frac{10^{-3}}{(6370 + 400)} \right]$$

$$U_{0 \rightarrow 1} = \frac{1}{2}mv_1^2 - \frac{1}{2}mv_0^2$$

$$\Rightarrow v_1^2 = \left(\frac{36000 \times 10^3}{3600} \right)^2 + 2(9.81)(6370 \times 10^3)^2 \left[\frac{10^{-3}}{(6370 + 1300)} - \frac{10^{-3}}{(6370 + 400)} \right]$$

$$\Rightarrow v_1 = 9284.5 \text{ m/s} = 33424 \text{ km/hr}$$

$$20. F_x = -\frac{\partial V}{\partial x} = -(10z + y)$$

$$F_y = -\frac{\partial V}{\partial y} = -(x + 15yz)$$

$$F_z = -\frac{\partial V}{\partial z} = -\left(10x + \frac{15y^2}{2}\right)$$

$$\mathbf{F} = -(10z + y)\mathbf{i} - (x + 15yz)\mathbf{j} - \left(10x + \frac{15}{2}y^2\right)\mathbf{k}$$

$$21. \frac{\partial F_x}{\partial y} = 0$$

$$\frac{\partial F_y}{\partial x} = 2 \neq \frac{\partial F_x}{\partial y}$$

因此 \mathbf{F} 不是保守力。

$$22. U_{1 \rightarrow 2} = \Delta T + \Delta V - F$$

$$180(2.5) = \frac{1}{2}(3 + 7 + 10)v^2 + 0 - (0.2)(3 + 7 + 10)g(2.5)$$

$$\Rightarrow v = 5.93 \text{ m/s}$$

$$23. 2y_A + y_B = \text{常數}$$

$$\therefore 2\dot{y}_A + \dot{y}_B = 0 \Rightarrow 2\Delta y_A = -\Delta y_B$$

$$T_2 - T_1 = V_1 - V_2$$

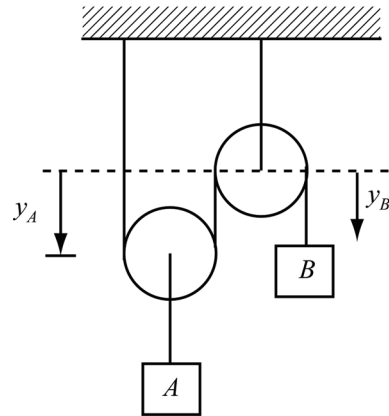
$$\Rightarrow \frac{1}{2}(3 + 2)\dot{y}_A^2 + \frac{1}{2}(10)(\dot{y}_B)^2 - 0$$

$$= 10(9.81)(3) - (3 + 2)(9.81)(1.5)$$

$$\frac{45}{2}\dot{y}_A^2 = (22.5)(9.81)$$

$$\Rightarrow \dot{y}_A = 3.13 \text{ m/s } \uparrow$$

$$\dot{y}_B = 6.26 \text{ m/s } \downarrow$$



$$24. T_1 + V_1 - L = T_2 + V_2$$

$$\frac{1}{2}(15 \times 10^{-3})(600)^2 - L = 0 + \frac{1}{2}(4500)(0.5)^2$$

$$\Rightarrow L = 2137.5 \text{ J}$$

$$25. x^2 + y^2 = 1 \Rightarrow 2x\dot{x} + 2y\dot{y} = 0 \Rightarrow \dot{x} = -\frac{y}{x}\dot{y}$$

$$T_1 + V_1 = T_2 + V_2$$

(1) $y = 2x$ 時, $y = \frac{2}{\sqrt{5}}, x = \frac{1}{\sqrt{5}}$

$$y = x \text{ 時, } y = \frac{1}{\sqrt{2}} = x$$

$$\therefore 0 + mg\left(\frac{2}{\sqrt{5}} - \frac{1}{\sqrt{2}}\right) = \frac{1}{2}m\dot{y}^2 + \frac{1}{2}m\dot{y}^2$$

$$\Rightarrow \dot{y} = 1.36 \text{ m/s} = \dot{x}$$

(2) $y = 0, \therefore \dot{x} = 0$

$$0 + mg\left(\frac{2}{\sqrt{5}}\right) = \frac{1}{2}m\dot{y}^2$$

第 5 章

計算題

1. (1) 動量 = $mv_0 = 10(1) = 10 \text{ kgms}^{-1}$

(2) 衝量 = $\int_0^{20} P dt = \frac{1}{2}(50)(20) = 500 \text{ N} \cdot \text{s}$

(3) $mv_0 + \int_0^{20} P dt = mv_f \Rightarrow v_f = \frac{10 + 500}{10} = 51 \text{ m/s}$

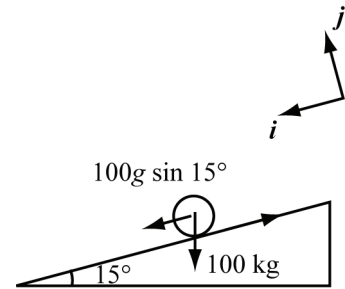
2. $20(3\mathbf{i} + 4\mathbf{j}) + \int_0^5 (0.5t^2\mathbf{i} + 0.1t\mathbf{j}) dt = 20\mathbf{v}_f \Rightarrow \mathbf{v}_f = (4\mathbf{i} + 4.1\mathbf{j}) \text{ m/s}$

3. $20 \text{ km/hr} \approx 5.56 \text{ m/s}$

$100(5.56) - \int_0^5 F dt = 0 \Rightarrow F = 111.1 \text{ N}$

4. 下坡 i 方向之動量 - 衝量原理

$100(5.56) + \int_0^T (100g \sin 15^\circ - 333.3) = 0 \Rightarrow T = 7 \text{ s}$



5. (1) 最大靜摩擦 = $0.55(25g) \text{ N} = 134.9 \text{ N}$

所以方塊在 $F > 134.9 \text{ N}$ 才開始滑動，
此時 $t = 8.1 \text{ s}$

(2) 動摩擦力 = $0.35(25g) \text{ N} = 85.8 \text{ N}$

所以，方塊在 24.85 s 後，施力小於動摩擦，方塊開始減速，
所以方塊最高速發生在 24.8 s 。

動量衝量原理：

$$25(0) + \int_0^{24.85} F dt - \int_0^{8.1} 134.9 dt - \int_{8.1}^{24.85} 85.8 dt = 25v$$

$$\frac{250(15)}{2} + \frac{250(9.85)}{2} - (134.9)(8.1) - 85.8(24.85 - 8.1) = 25v$$

$\Rightarrow v = 23.1 \text{ m/s}$

6. 最高速度： $F - R = 0 \Rightarrow v = \sqrt{\frac{F}{k}}$

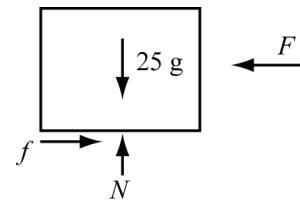
此時間內之動量衝量關係

$$m(0) + \int_0^T (F - kv^2) dt = mv$$

所以總衝量 = $\int_0^T (F - kv^2) dt = mv = m\sqrt{\frac{F}{k}}$

7. 水平方向動量衝量原理

$10(5 \cos 25^\circ) = (10 + 20)v_f \Rightarrow v_f = 1.51 \text{ m/s}$



8. 設大三角之絕對速度為 v 水平往左，
則 B 之絕對速度為 $(5 \cos 30^\circ - v)$ ，
動量守恆：

$$0 = 50v - 10(5 \cos 30^\circ - v)$$

$$\Rightarrow v = 0.72 \text{ m/s}$$

9. (1) $0 + F_{\text{平均}}(5) = 500 \left(\frac{30 \times 10^3}{3600} \right) \Rightarrow F_{\text{平均}} = 833.3 \text{ N}$

(2) $500 \left(\frac{30 \times 10^3}{3600} \right) + 0 = (15500)v \Rightarrow v = 0.27 \text{ m/s} \rightarrow$

船速同汽車往碼頭以 0.27 m/s 前進。

10. 運動學關係：

$$v_N = 2v_M$$

水平方向

$$0 + [2T - 0.2(50)(9.81)]5 = 50v_M \quad (\text{i})$$

垂直方向

$$0 + (10g - T)(5) = 10v_N \quad (\text{ii})$$

$$(\text{i}) \& (\text{ii}) \Rightarrow v_N = 10.9 \text{ m/s}$$

11. 嵌入後速度 v

$$10(500) = 510(v) \Rightarrow v = 9.8039 \text{ m/s}$$

所以系統動能為

$$\frac{1}{2}(0.51)(9.8039)^2 = 24.51 \text{ J}$$

系統首度靜止時木塊移動 $x \text{ m}$ ，則能量平衡

$$\frac{1}{2}(1000)x^2 - 0.5(0.51)(9.81)(x) = 24.51$$

$$\Rightarrow x = 0.224 \text{ m}$$

12. 水平方向

$$20(80) = 8(160) \cos \theta + 12(v) \cos 52^\circ$$

垂直方向

$$8(160) \sin \theta - 12(v) \sin 52^\circ = 0$$

解上述二式得

$$\theta = 47.7^\circ$$

$$v = 100 \text{ m/s}$$

13. (1) 動量守恆

$$4(4.5) + 1.5(-1.5) = 4(v_{Mf}) + 1.5(v_{Nf}) \quad (\text{i})$$

$$0.75 = -\frac{v_{Nf} - v_{Mf}}{-1.5 - 4.5} \quad (\text{ii})$$

$$(\text{i}) \Rightarrow 4v_{Mf} + 1.5v_{Nf} = 15.75 \quad (\text{iii})$$

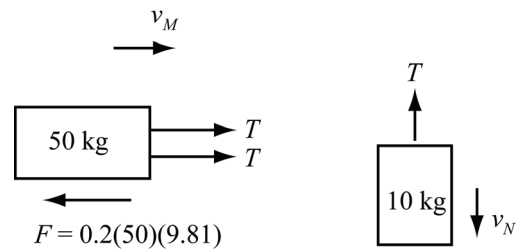
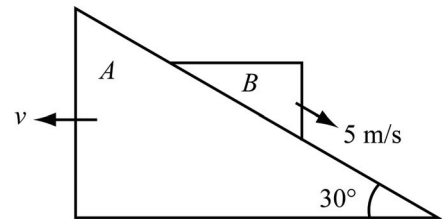
$$(\text{ii}) \Rightarrow v_{Nf} - v_{Mf} = +4.5 \quad (\text{iv})$$

$$(\text{iii}) \& (\text{iv}) \Rightarrow v_{Mf} = 1.636 \text{ m/s}$$

$$v_{Mf} = 1.636 \text{ m/s}$$

$$v_{Nf} = 6.14 \text{ m/s}$$

(ii) 能量損失：



$$\frac{1}{2}4(4.5)^2 + \frac{1}{2}(1.5)(1.5)^2 - \frac{1}{2}(4)(1.636)^2 - \frac{1}{2}(1.5)(6.14)^2 = 8.56 \text{ J}$$

14. (1) 動量守恆

$$4v_{Pi} + 6(2) = 6(5) + 4v_{Pf} \quad (\text{i})$$

恢復係數

$$0.5 = \frac{v_{Pf} - 5}{2 - v_{Pi}} \Rightarrow 1 - 0.5v_{Pi} = v_{Pf} - 5 \quad (\text{ii})$$

$$(\text{i}) \& (\text{ii}) \Rightarrow v_{Pi} = 7 \text{ m/s}$$

$$v_{Pf} = 2.5 \text{ m/s}$$

$$(2) \quad 6(2) + F(0.003) = 6(5) \Rightarrow F = 6000 \text{ N}$$

15. 碰撞前相對速度 $v_i = \sqrt{2g(0.5)}$

$$\text{碰撞後相對速度 } v_f = \sqrt{2g(0.078)}$$

$$\text{恢復係數} = \frac{v_f}{v_i} = \sqrt{\frac{0.078}{0.5}} = 0.395$$

16. 撞擊前 A 之速度： $v = \sqrt{2(9.81)(1)} = 4.43 \text{ m/s}$

$$\text{動量守恆：} 10(4.43) = 20v_f \Rightarrow v_f = 2.215 \text{ m/s}$$

設壓縮量為 h ，能量守恆

$$\frac{1}{2}(20)(2.215)^2 + 20(9.81)h = \frac{1}{2}(1000)h^2 \Rightarrow h = 0.566 \text{ m}$$

17. 由 15 題知 $e = \sqrt{\frac{h_{n+1}}{h_n}}$

$$\therefore \frac{h_1}{2} \frac{h_2}{h_1} = e^4 \Rightarrow h_2 = 2(0.8)^4 = 0.82 \text{ m}$$

18. 碰撞前速度分量

$$(v_P)_n = 10 \cos 60^\circ = 5 \text{ i m/s}$$

$$(v_P)_t = 10 \sin 60^\circ = 8.66 \text{ j m/s}$$

$$(v_Q)_n = -5 \cos 30^\circ = -4.33 \text{ i m/s}$$

$$(v_Q)_t = 5 \sin 30^\circ = 2.5 \text{ j m/s}$$

碰撞後 P 、 Q 在 n 方向之速度分量為 $(v_{Pf})_n \text{ i}$ 及 $(v_{Qf})_n \text{ i}$

動量守恆：

$$1(5) - 2(4.33) = 1(v_{Pf})_n + 2(v_{Qf})_n$$

$$\Rightarrow (v_{Pf})_n + 2(v_{Qf})_n = -3.66 \quad (\text{i})$$

恢復係數

$$0.8 = \frac{(v_{Qf})_n - (v_{Pf})_n}{5 - (-4.33)}$$

$$\Rightarrow (v_{Qf})_n - (v_{Pf})_n = 7.464 \quad (\text{ii})$$

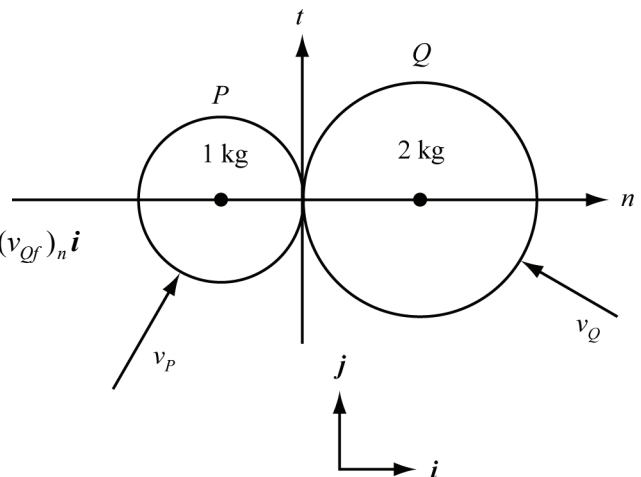
(i)&(ii)

$$(v_{Qf})_n = 1.268 \text{ m/s}$$

$$(v_{Pf})_n = -6.196 \text{ m/s}$$

$$\therefore \mathbf{v}_{Pf} = (-6.2\mathbf{i} + 8.66\mathbf{j}) \text{ m/s}$$

$$\mathbf{v}_{Qf} = (1.27\mathbf{i} + 2.5\mathbf{j}) \text{ m/s}$$



19. (1) 球 P 在剛碰撞前之速度 $=\sqrt{2g} = 4.43 \text{ m/s} \downarrow$

碰撞前後 P 及 Q 的速度分量

$$(v_{Pi})_n = 4.43 \cos 30^\circ = 3.836 \text{ m/s}$$

$$(v_{Pi})_t = -4.43 \sin 30^\circ = -2.215 \text{ m/s}$$

$$(v_{Qi})_n = 0, \therefore (v_{Qi})_t = 0$$

因受繩子拘束，故

$$(v_{Qf}) = v_{Qf} \mathbf{i}$$

$$\therefore (v_{Qf})_n = v_{Qf} \sin 30^\circ = 0.5v_{Qf}$$

$$(v_{Qf})_t = v_{Qf} \cos 30^\circ = 0.866v_{Qf}$$

因為有繩子拘束，碰撞時會施力衝力，故動量不守恆。

球 P 在 t 方向無外加衝力

$$(v_{Pi})_t = (v_{Pf})_t = -2.215 \text{ m/s}$$

設 T 為繩子所施加之衝力，則球 P 與 Q 之動量衝量關係

$$m\mathbf{v}_{Pi} + m\mathbf{v}_{Qi}^0 + T\Delta t = m\mathbf{v}_{Pf} + m\mathbf{v}_{Qf}$$

i 方向

$$0 = m(v_{Pf})_n \sin 30^\circ + m(v_{Pf})_t \cos 30^\circ + m(v_{Qf})$$

$$\Rightarrow 0 = 0.5(v_{Pf})_n - 1.918 + v_{Qf} \quad (\text{i})$$

因球為彈性，故恢復係數為 1

$$\therefore (v_{Qf})_n - (v_{Pf})_n = (v_{Pi})_n - (v_{Qi})_n$$

$$0.5v_{Qf} = (v_{Pf})_n = 3.836 - 0 \quad (\text{ii})$$

$$\text{(i)\&(ii)} \Rightarrow (v_{Pf})_n = -2.3 \text{ m/s}$$

$$v_{Qf} = 3.0688 \text{ m/s}$$

所以，球 P 碰撞後速度：

$$v_{Pf}^2 = (2.215)^2 + (2.3)^2$$

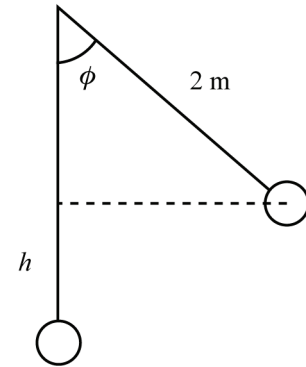
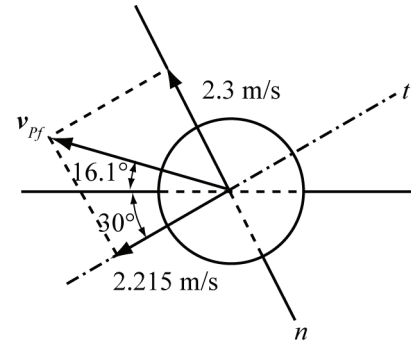
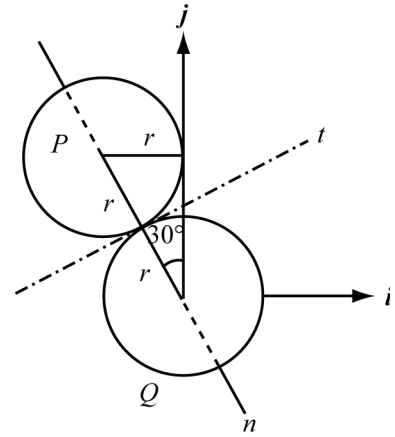
$$\Rightarrow v_{Pf} = 3.19 \text{ m/s 與水平成 } 16.1^\circ$$

(2) 球 Q 能量守恆：

$$\frac{1}{2}m(v_{Qf})^2 = mgh$$

$$\Rightarrow h = \frac{(3.0688)^2}{2(9.81)} = 0.48 \text{ m}$$

$$\Rightarrow \phi = \cos^{-1} \frac{(2 - 0.48)}{2} = 40.5^\circ$$



20. 撞擊前後之速度分量

$$(v_{Pi})_n = 5 \cos 30^\circ = 4.33 \text{ m/s}$$

$$(v_{Pi})_t = 5 \sin 30^\circ = -2.5 \text{ m/s}$$

$$(v_{Qi})_n = (v_{Qi})_t = 0$$

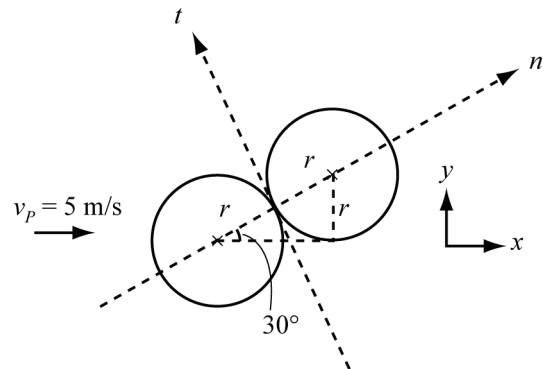
碰撞後

$$(v_{Pf})_t = (v_{Pi})_t = -2.5 \text{ m/s}$$

$$(v_{Qf})_t = 0$$

n 方向碰撞前後動量守恆

$$m(v_{Pi})_n + m(v_{Qi})_n = m(v_{Pf})_n + m(v_{Qf})_n$$



$$\Rightarrow 4.33 = (v_{Pf})_n + (v_{Qf})_n \quad (i)$$

球為彈性，所以

$$(v_{Pi})_n - (v_{Qi})_n = (v_{Qf})_n - (v_{Pf})_n$$

$$\Rightarrow 4.33 = (v_{Qf})_n - (v_{Pf})_n$$

$$\Rightarrow \therefore (v_{Qf})_n = 4.33 \text{ m/s}$$

$$(v_{Pf})_n = 0 \text{ m/s}$$

$$\therefore (v_{Qf})_x = 4.33 \cos 30^\circ = 3.75 \text{ m/s}$$

$$(v_{Qf})_y = 4.33 \sin 30^\circ = 2.165 \text{ m/s}$$

$$\therefore x = 3.75 \frac{(2)(2.165)}{g} = 1.655 \text{ m}$$

21. (1) 系統的總動量 $\sum_{i=1}^3 \mathbf{L}_i$

$$\begin{aligned} \sum_{i=1}^3 \mathbf{L}_i &= 3(9\mathbf{i}) + 5(4\mathbf{j} + 5\mathbf{k}) + 6(3\mathbf{i} + 7\mathbf{k}) \\ &= (45\mathbf{i} + 20\mathbf{j} + 67\mathbf{k}) \text{ kgms}^{-1} \end{aligned}$$

(2) 總角動量 $\sum_{i=1}^3 \mathbf{H}_{oi}$

$$\begin{aligned} \sum_{i=1}^3 \mathbf{H}_{oi} &= \sum_{i=1}^3 \mathbf{r}_i \times m\mathbf{v}_i = (3\mathbf{i} + 3\mathbf{j}) \times 27\mathbf{i} + (2\mathbf{i} - \mathbf{j} + \mathbf{k}) \times (20\mathbf{j} + 25\mathbf{k}) + (\mathbf{i} + \mathbf{j} + \mathbf{k}) \times (18\mathbf{i} + 42\mathbf{k}) \\ &= -81\mathbf{k} - 45\mathbf{i} - 50\mathbf{j} + 40\mathbf{k} + 42\mathbf{i} - 24\mathbf{j} - 18\mathbf{k} \\ &= (-3\mathbf{i} - 74\mathbf{j} - 59\mathbf{k}) \text{ kgm}^2\text{s}^{-1} \end{aligned}$$

22. (1) A 之速度

$$\begin{aligned} \mathbf{v}_A &= (5 \cos 30^\circ \mathbf{i} + 5 \sin 30^\circ \mathbf{j}) + (\sin 30^\circ \mathbf{i} - \cos 30^\circ \mathbf{j}) \\ &= (4.83\mathbf{i} + 1.63\mathbf{j}) \text{ m/s} \end{aligned}$$

$$\text{所以 } A \text{ 之動量} = m\mathbf{v}_A = (9.66\mathbf{i} + 3.27\mathbf{j}) \text{ kgms}^{-1}$$

(2) $\mathbf{H}_{OA} = \mathbf{r}_{OA} \times \mathbf{v}_A$

$$\begin{aligned} &= (0.5 \cos 30^\circ \mathbf{i} + 0.5 \sin 30^\circ \mathbf{j}) \times (4.83\mathbf{i} + 1.63\mathbf{j}) \\ &= -0.5\mathbf{k} \text{ kgm}^2\text{s}^{-1} \end{aligned}$$

(3) $\dot{\mathbf{H}}_{OA} = \sum \mathbf{M}_O = \mathbf{r}_{OA} \times m\mathbf{a}_A$

$$\mathbf{r}_{OA} = 0.5\mathbf{e}_r$$

$$\mathbf{a}_A = (\ddot{r} - r\dot{\theta}^2)\mathbf{e}_r + (r\ddot{\theta} + 2\dot{r}\dot{\theta})\mathbf{e}_\theta$$

$$\therefore \sum \mathbf{M}_O = 0.5\mathbf{e}_r \times [(\ddot{r} - r\dot{\theta}^2)\mathbf{e}_r + (r\ddot{\theta} + 2\dot{r}\dot{\theta})\mathbf{e}_\theta]$$

$$= 0.5(r\ddot{\theta} + 2\dot{r}\dot{\theta})\mathbf{k}$$

$$= 0.5(0.5(0) + 2(5)(2))\mathbf{k}$$

$$= 10\mathbf{k} \text{ N} \cdot \text{m}$$

$$\therefore \dot{\mathbf{H}}_{OA} = 10\mathbf{k} \text{ N} \cdot \text{m}$$

