

Final Examination (Dynamics of Machine Systems)

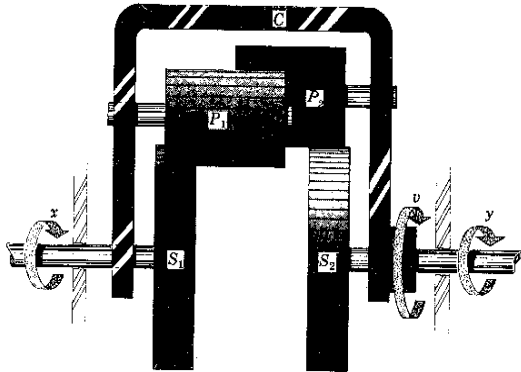
Upload deadline: 2026/6/23 24:00

1. Calculate the Mobility (DOF) of the 2-D or 3-D mechanical system : (15%)

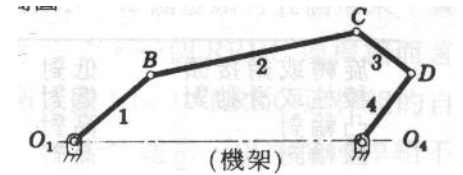
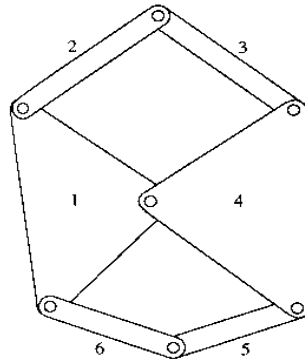
(a) Spur-gear differential

(b) Watt six-bar linkage

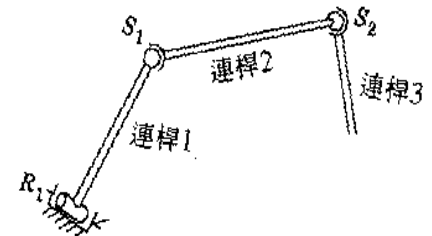
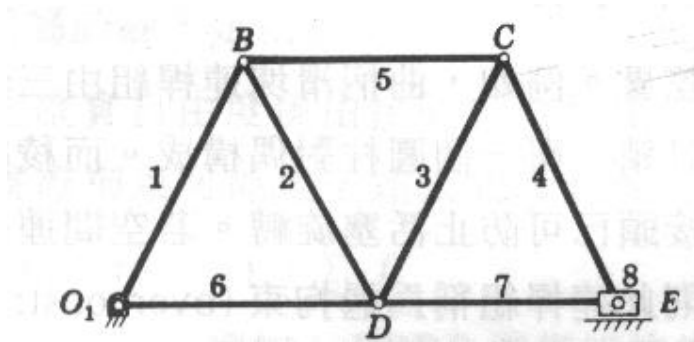
(c) Five-bar linkage



(d) Truss structure



(e) Spatial robotics



2. Find the 4-bar linkage with the dimensions of (a) and (b). Please use Grashoff's theorem to determine the type of four-bar mechanism, if the link#1 is fixed. Please also solve for the transmission angle and output angle. (20%)

(a) $r_1=1\text{m}$, $r_2=2\text{m}$, $r_3=1.5\text{m}$, $r_4=3.5\text{m}$; when $\theta_2=120^\circ$, solve for the transmission angle and output angle .

(b) $r_1=5\text{cm}$, $r_2=10\text{cm}$, $r_3=15\text{cm}$, $r_4=15\text{cm}$; when $\theta_2=270^\circ$, solve for the transmission angle and output angle .

3. As shown in the Fig. 1, the pendulum(OA) has the initial angle 210° with respect to horizontal positive x-axis. If the pendulum has mass $m=5\text{kg}$, length $l=10\text{m}$, gravity $g=9.8\text{m/s}^2$ and release from an initial angular velocity 1 rad/s . Please solve for the angular acceleration and reaction force of revolute joint O at the release instant. (10%)

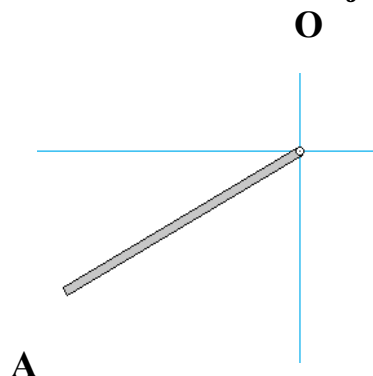


Fig. 1

4. The 4-Bar-Linkage as shown in Fig. 2, Link#2 rotates with constant angular velocity $\omega_2 = 1 \text{ rad/s (CCW)}$. If $O_2O_4=20\text{mm}$, $O_2A=20\text{mm}$, $O_4B=40\text{mm}$. Link#2(O_2A) and Link#4(O_4B) are perpendicular to the horizontal axis. Please use complex analysis method to solve for Link#3(AB) and Link#4(O_4B) angular velocities ω_3 and ω_4 , also the angular accelerations α_3 and α_4 . (15%)

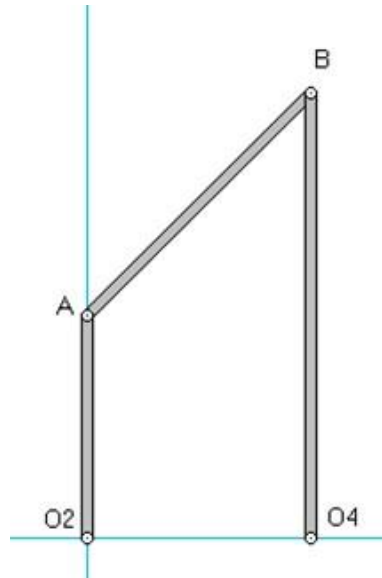


Fig. 2

5. A 3mm module, 20° pinion of 18 teeth drives a gear of 45 teeth. The pinion rotates with an angular velocity 9 rad/s (CCW). Calculate (A) Radius of pitch circle (B) Radius of base circle (C) Dedendum (D) Addendum (E) Diametral pitch (F) Center distance (G) The angular velocity of gear (magnitude and direction) (H) Base pitch (I) Length of action (J) Contact Ratio. (20%)
6. A 0.3-module pinion of 34 teeth drives a gear with 60 teeth. If the center distance is increased by 0.127 mm, compare the backlash produced with pressure angles of 14.5° , 20° , and 25° . (10%)
7. A three-threaded worm drives a 35-tooth worm gear having a pitch diameter of 207.8 mm and a helix angle of 21.08° . If the shafts are at right angles, calculate the lead and the pitch diameter of the worm. (10%)
8. A planetary gear train for a two-speed aircraft supercharger drive is shown in Fig. 3. Gear 2 is driven by a 63-tooth gear (not shown) which operates at 2400 rpm. At high speed, gear 2 connects to the supercharger shaft through additional gearing. At low speed, gear 7 is held stationary and shaft B is connected to supercharger shaft with the same gear ratio as was used between gear 2 and the supercharger shaft. If the supercharger operates 24000 rpm at high speed, calculate the low speed value. (10%)

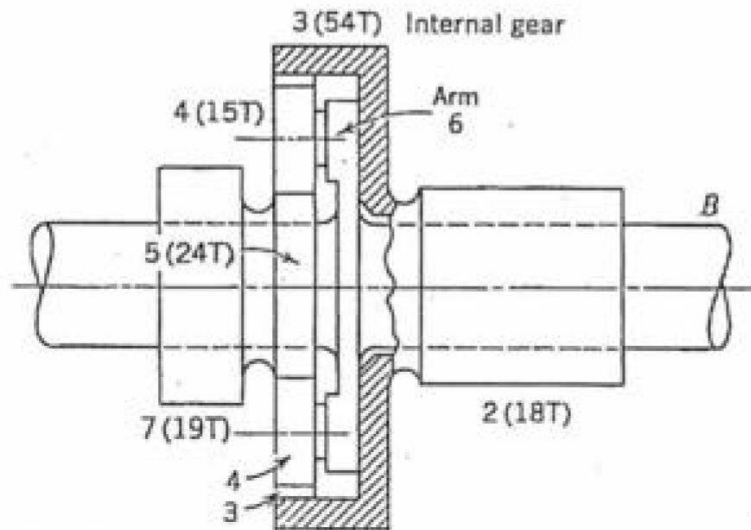


Fig. 3

9. In the planetary reduction unit shown in Fig. 4, gear 2 turns at 300 rpm in the direction indicated. Determine the speed and direction of rotation of gear 5. (10%)

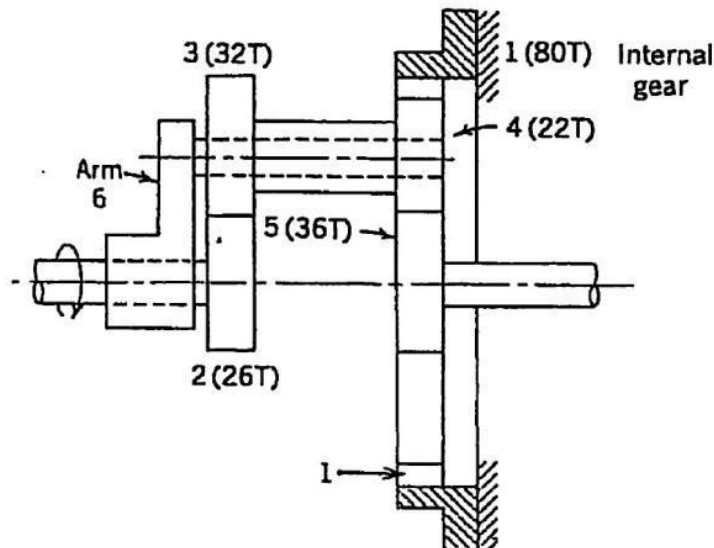


Fig. 4

1. Please submit the solution of final examination before 2026/6/23 24:00.
2. Please upload your document file(*.docx) and insert hand-writing file (please scan to the image file save as JPG file) to the following website.

Host Name: 140.130.17.62

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Please go to directory \Final-Examination, you can use your student ID to create a subdirectory. Finally, you should upload your files to your student ID subdirectory.